

Systems and Control Theory

Master Degree Course in ELECTRONICS ENGINEERING

<http://www.dii.unimore.it/~lbiagiotti/SystemsControlTheory.html>

A General Introduction to Matlab

Luigi Biagiotti

e-mail: luigi.biagiotti@unimore.it

<http://www.dii.unimore.it/~lbiagiotti>

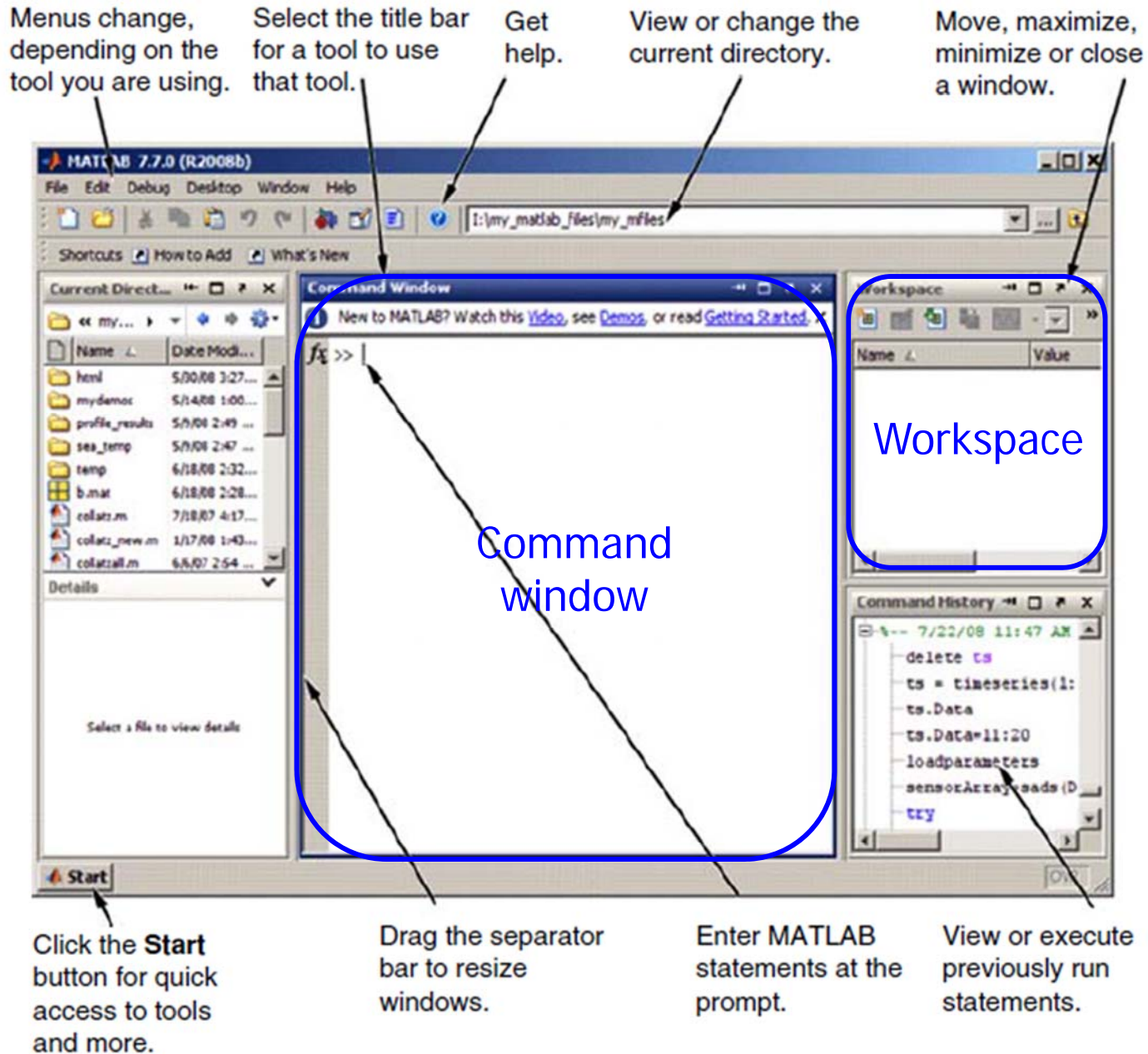
Outline

- The objectives of this lecture are
 - To become familiar with the MATLAB environment
 - To enable you to use some simple MATLAB commands from the *Command Window*
- Bibliography:
 - Brian Hahn and Daniel T. Valentine, *Essential MATLAB for Engineers and Scientists*, Academic Press.

Matlab

- MATLAB is a powerful computing system for handling scientific and engineering calculations.
- The name MATLAB stands for **Matrix Laboratory**, because the system was designed to make matrix computations particularly easy.
- Matlab is based on a kernel of **general purpose functions** enhanced with additional tools, the so-called **Toolboxes**, that help users to solve specific problems, e.g. the Control System Toolbox. A toolbox is a simple collection of matlab functions.

Matlab Desktop



Command Window



```
MATLAB Command Window
File Edit View Window Help

This version is for educational classroom use only.

To get started, type one of these: helpwin, helpdesk, or demo.
For product information, type tour or visit www.mathworks.com.

>> pwd
ans =
C:\MATLABR11\work

>> dir
.
..
notoreDC0.n      notoreDC@plot.n
notoreDC@nd1.mdl

>> dir *.n
notoreDC0.n      notoreDC@plot.n

>> notoreDC0
elapsed_time =
    0.4868

>> who
Your variables are:

Anp      Kgf      U        h        rad
Cn       Kn       Ucen     lu       rpr
Cnax     Lne     UI       n        s
Cr       N        Un       nAnp     t
Henry    Nm       Wmax     nHenry   th
ic0      Ona     Wne     nN       th0
Inax     Rne0    Wne0     ng       tip0
Ine      TABCR   bne     minuti   tout
Ine0     TABTEPI cm       m
Jne      TABVIN  q       nSec
KI       Tcsin   gr       nprova
Kg       Tfin    gradi   ora

>> edit notoreDC0
>> cd d:
>> pwd
ans =
D:\

>> clc
Ready
```

- **MATLAB commands must be inserted by means of the Command Window.**
- Some commands of general use are
 - **pwd** provides the current directory
 - **dir** lists the files of current directory
 - **clc** clears the command window
- Variables defined in the MATLAB environment are collected in the **Workspace**. **who** lists the variables in the current workspace. Command **clear** removes all variables from the workspace.
- Command **help** provides the list of all the toolboxes which are installed in the system. By typing in
>> help <toolbox name>
one obtains the list of the functions composing the toolbox (e.g. help control). The command
>> help <command name>
provides a description of this command

Variables

- MATLAB variables are created with an assignment statement

```
>> variable name = a value (or an expression)
```

where *expression* is a combination of numerical values, mathematical operators, variables, and function calls

- For example

```
>> x=12;<ENTER>
```

By omitting the semicolon (;) the name and the value of the variable are printed in the screen. Conversely, the *echo* of the command is not provided

- Once a variable has been created, it can be reassigned

```
>> t = 5; <----- The intermediate result is not shown
```

```
>> t = t+1
```

```
    t =
```

```
    6
```

Error messages

- If we enter an expression incorrectly, MATLAB will return an error message.
- For example

```
>> x = 10;
```

```
>> 5x
```

```
??? 5x
```

```
|
```

```
Error: Unexpected MATLAB expression.
```

Basic mathematical functions

Trigonometric.

<code>sin</code>	- Sine
<code>sinh</code>	- Hyperbolic sine.
<code>asin</code>	- Inverse sine.
<code>cos</code>	- Cosine.
<code>cosh</code>	- Hyperbolic cosine.
<code>acos</code>	- Inverse cosine.
<code>tan</code>	- Tangent.
<code>tanh</code>	- Hyperbolic tangent.
<code>atan</code>	- Inverse tangent.
<code>atan2</code>	- Four quadrant inverse tangent.

Exponential.

<code>exp</code>	- Exponential.
<code>log</code>	- Natural logarithm.
<code>log10</code>	- Common (base 10) logarithm.
<code>sqrt</code>	- Square root.

Complex.

<code>abs</code>	- Absolute value.
<code>angle</code>	- Phase angle.

Rounding and remainder.

<code>floor</code>	- Round towards minus infinity.
<code>ceil</code>	- Round towards plus infinity.
<code>round</code>	- Round towards nearest integer.
<code>mod</code>	- Modulus (signed remainder after division).
<code>rem</code>	- Remainder after division.
<code>sign</code>	- Signum.

MATLAB offers many predefined mathematical functions for technical computing.

Typing **help elfun** and **help specfun** calls up full lists of elementary and special functions that are built into MATLAB..

Note that trigonometric functions work in radians

Predefined constant values

- In addition to the elementary functions, MATLAB includes a number of predefined constant values. The most common values are:
 - **pi** ←----- The π number, $\pi = 3.14159$
 - **i, j** ←----- The imaginary unit i
 - **Inf** ←----- The infinity, ∞
 - **NaN** ←----- Not a number

Matrices and vectors

- To type a matrix into MATLAB it is necessary to
 - begin with a square bracket, `[`
 - separate elements in a row with spaces or commas (`,`)
 - use a semicolon (`;`) to separate rows
 - end the matrix with another square bracket, `]`.
- Example

```
>> A=[1,2,3;4,5,6;7,8,9]
```

```
A =
```

```
    1    2    3
    4    5    6
    7    8    9
```

Matrices and vectors

- A vector is a special case of a matrix

```
>> c=[4;5;6]
```

```
c = ←----- column
      vector
      4
      5
      6
```

```
>> r=[4,5,6]
```

```
r = ←----- row vector
      4      5      6
```

- A row vector can be converted to a column vector using the transpose operator, and vice-versa. The transpose operation is denoted by an apostrophe or a single quote (').
- The easiest way of defining a vector where the elements (components) increase by the same amount is

```
>> t=[0:0.1:10] ←----- row vector with elements from 0
                       to 10 with step 0.1
```

Matrices and vectors indexing

- Once we have entered a matrix, we can refer to it simply as matrix **A**. We can then view a particular element in a matrix by specifying its location

```
>> Element = A(2,1)
```

Note that the indices start from 1

```
Element =
```



```
4
```

- Correcting any entry is easy through indexing

```
>> A(3,3) = 0
```

```
A =
```

```
1    2    3
4    5    6
7    8    0
```

Here we substitute $A(3,3)=9$
by $A(3,3)=0$

The colon operator (:)

- The colon operator can be used to pick out a certain row or column. For example, the statement `A(m:n,k:l)` specifies rows `m` to `n` and column `k` to `l`.

- Example 1

```
>> A(1,:)
```

```
ans =
```

```
    1    2    3  <----- First row of A
```

- Example 2

```
>> A(:,1)
```

```
ans =
```

```
    1
```

```
    4
```

```
    7
```

```
<----- First column of A
```

- Example 3

```
>> B=A(2:3,1:2)
```

```
B =
```

```
    4    5
```

```
    7    8
```

```
<----- Sub-matrix of A
```

Matrix generators

MATLAB provides functions that generate elementary matrices:

`A=eye(n);` \leftarrow ----- n-by-n identity matrix

`A=eye(n,m);` \leftarrow ----- m-by-n matrix with 1 on the main diagonal

`A=zeros(m,n);` \leftarrow ----- m-by-n matrix of zeros

`A=ones(m,n);` \leftarrow ----- m-by-n matrix of ones

`A=rand(m,n);` \leftarrow ----- m-by-n matrix of random numbers

`A=diag(V);` \leftarrow ----- n-by-n matrix with the element of vector \mathbf{v} on the main diagonal

For a complete list of *elementary matrices* and *matrix manipulations*, type `help elmat` or `doc elmat`

Concatenating matrices

- Matrices can be made up of sub-matrices
- **Problem:** make up the 6-by-6 matrix

$$A = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \quad \text{where} \quad \begin{aligned} A_{11} &= [v_1, v_2, v_3] \\ A_{12} &= \mathbf{0}_3 \\ A_{21} &= I_3 \\ A_{22} &= [v_3, v_2, v_1] \end{aligned}$$

and v_1, v_2 e v_3 are column vetors defined by the user.

- **Solution:**

```
>> v1 = [1 2 3]';  
>> v2 = rand(3,1);  
>> v3 = [3; 2; 1];  
>> A11=[v1 v2 v3];  
>> A22=[v3 v2 v1];  
>> A = [A11, eye(3); zeros(3), A22]
```

Array operations

- MATLAB allows the following arithmetic operations on matrices:

- addition +

```
>> A+B
```

- subtraction -

```
>> A-B
```

valid if **A** and **B** are of the same size

- multiplication *

```
>> A*B
```

valid if **A**'s number of column equals **B**'s number of rows

- (right and left) divisions / \

```
>> A/B
```

Equivalent to
A*inv(B)

```
>> A\B
```

Equivalent to
inv(A)*B

- Exponentiation ^

```
>> A^2
```

valid if **A** is square and equals **A*A**

Operations element-by-element

- Arithmetic operations can be done *element-by-element*. The period character (`.`) distinguishes these operations from standard matrix operations.

- multiplication `.*`

```
>> A.*B
```

- (right and left) divisions `./` `.\`

```
>> A./B
```

```
>> A.\B
```

 `A` and `B` are of the same size

- Exponentiation `.^`

```
>> A.^B
```

- Example:

```
>> v = [1 2 3].*[1 2 3]
```

```
v =
```

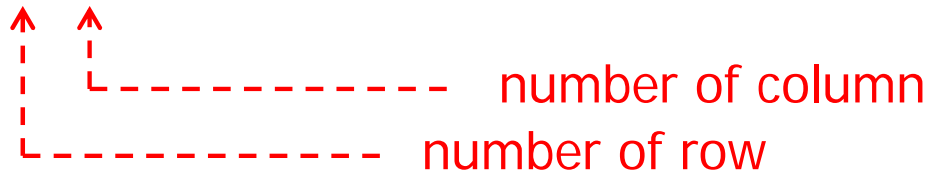
```
1    4    9
```

Matrix functions

MATLAB provides many matrix functions for various matrix/vector manipulations

- Dimensions

```
>> [m,n]=size(A)
```



number of column
number of row

for vectors, see command **length**

- Transpose

```
>> B=A' (alternatively >> B=transpose(A) )
```

- Determinant

```
>> d=det(A) <----- A must be square
```

Matrix functions

- Inverse

`>> I=inv(A)` `<----- A must be square`

For rectangular matrices, see command `pinv`

- Rank, i.e. number of linearly independent rows or columns

`>> r=rank(A)`

- Eigenvalues

`>> e=eig(A)`

↑
|

`Vector containing the
eigenvalues`

Solution of a linear system

- Problem: solve the system

$$\begin{cases} x_1 + x_2 + x_3 - x_4 = 1 \\ x_1 + x_2 - x_3 = 2 \\ x_1 - x_2 + x_3 = 0 \\ x_1 + 2x_2 - 3x_3 = 2 \end{cases}$$

- Solution:

```
>> A = [1, 1, 1, -1; 1, 1, -1, 0; 1, -1, 1, 0; 1, 2, -3, 0];  
>> b = [1, 2, 0, 2]';  
>> x = inv(A)*b;
```

or

```
>> x = A\b
```

Vectors role

- The vectors have in MATLAB two fundamental functions:
 - **polynomials representation**, a polynomial is represented by the vector of its coefficients
 - **signals representation**, a signal is represented by the sequence of values that it takes during time, therefore by a vector

Operations on polynomials

- Polynomial “pol” ($= 3s^2 + 2s + 1$) can be defined with the statement:

```
>> pol = [3 2 1]
```

```
pol =
```

```
3 2 1
```

- **roots**: roots computation (pol=0):

```
>> roots(pol)
```

```
ans =
```

```
-0.3333 + 0.4714i
```

```
-0.3333 - 0.4714i
```

- **polyval**: pointwise evaluation of a polynomial:

```
>> polyval(pol,1)
```

```
ans =
```

```
6
```

Operations on polynomials

- Computation of the residues, poles and direct term of the partial fraction expansion of the ratio of two polynomials:

es.

$$\frac{2s^3 + 5s^2 + 3s + 6}{s^3 + 6s^2 + 11s + 6} = \frac{-6}{s+3} + \frac{-4}{s+2} + \frac{3}{s+1} + 2$$

```
>> num = [2 5 3 6]; den = [1 6 11 6];
```

```
>> [r,p,k] = residue(num,den)
```

```
r =
```

```
   -6.0000
```

```
   -4.0000
```

```
    3.0000
```

```
p =
```

```
   -3.0000
```

```
   -2.0000
```

```
   -1.0000
```

```
k =
```

```
    2
```

Operations on polynomials

- **Polynomial multiplication** ($\text{pol3}=(s+1)(s+1)$):

```
>> pol1=[1 1]; pol2=[1 1];  
>> pol3=conv(pol1,pol2)  
pol3 =  
1 2 1
```

- **Polynomial division** ($(s^2+2s+2)=q(s)(s+1)+r(s)$):

```
>> pol1=[1 2 2]; pol2=[1 1];  
>> [q,r]=deconv(pol1,pol2)  
q =          <----- quotient  
1         1  
r =          <----- remainder  
0         0         1
```

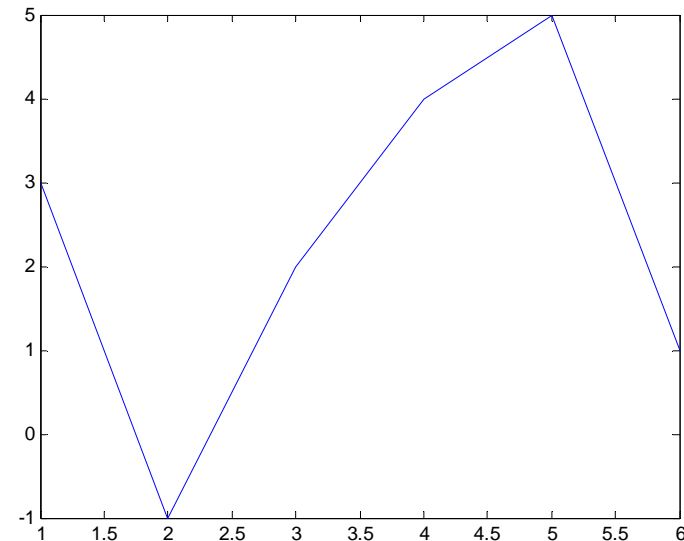

Basic plotting

- The basic MATLAB graphing procedure, for example in 2D, is to take a vector of x -coordinates, $x = (x_1, \dots, x_n)$, and a vector of y -coordinates, $y = (y_1, \dots, y_n)$, locate the points (x_i, y_i) , $i = 1, \dots, n$ and then join them by straight lines.
- This procedure is made by the command `plot`.

- Example:

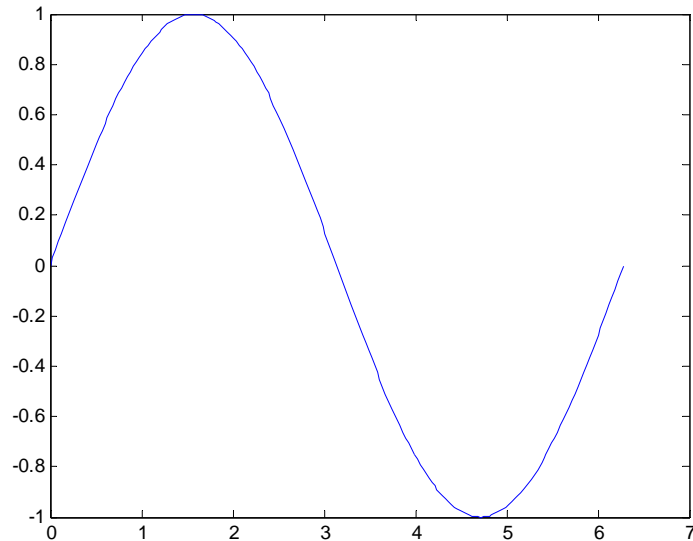
```
>> x = [1 2 3 4 5 6];  
>> y = [3 -1 2 4 5 1];  
>> plot(x,y)
```

x and y must have the same length



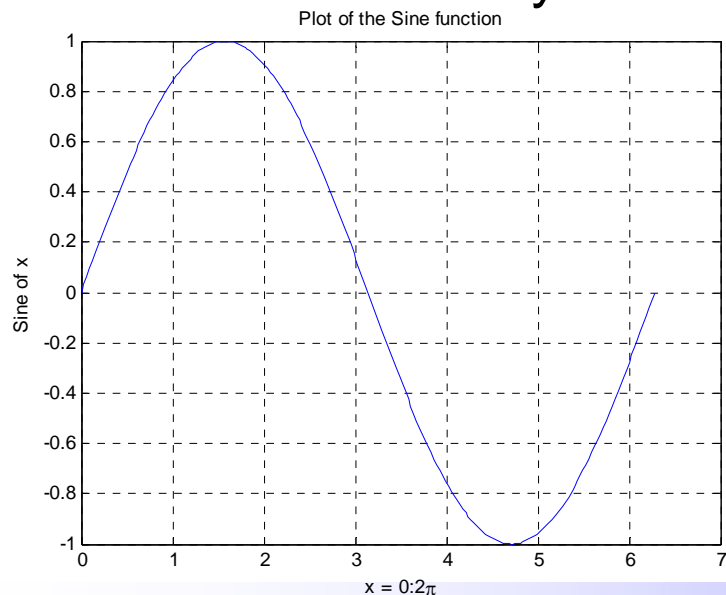
- **Problem:** plot the function `sin(x)` for x from 0 to 2π

Adding titles, axis labels, and annotations



```
>> x=0:0.1:2*pi;  
>> plot(x,sin(x))
```

- MATLAB enables you to add axis labels, titles, and a grid.



```
>> grid on  
>> xlabel('x = 0:2\pi')  
>> ylabel('Sine of x')  
>> title('Plot of the Sine function')
```

Specifying line styles and colors

- It is possible to specify line styles, colors, and markers (e.g., circles, plus signs, . . .) using the plot command:

```
plot(x,y,'style_color_marker')
```

where `style_color_marker` is a triplet of values from the following table

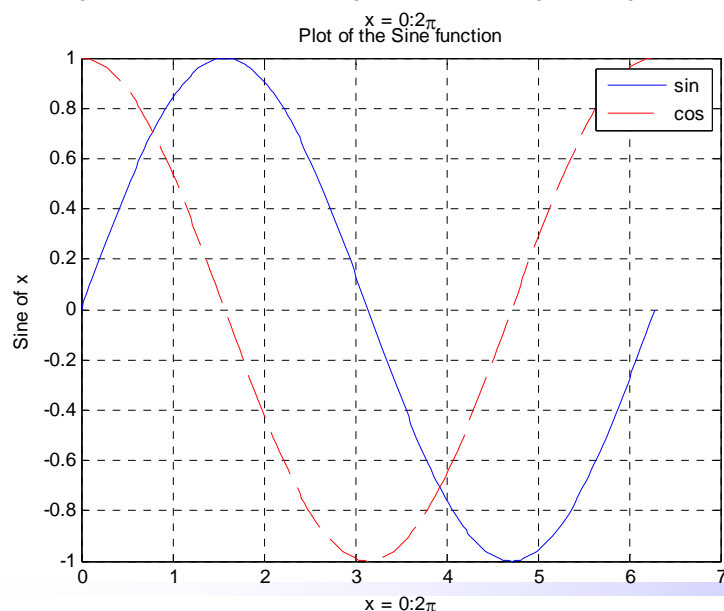
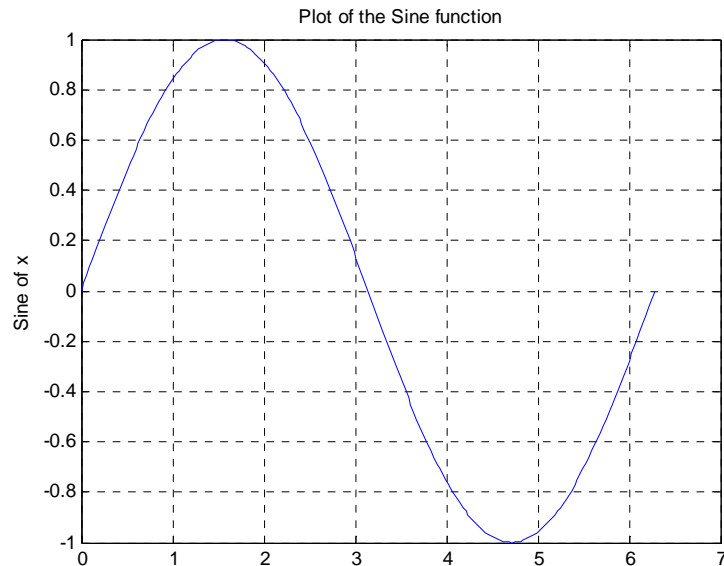
Symbol	Color
k	Black
r	Red
b	Blue
g	Green
c	Cyan
m	Magenta
y	Yellow

Symbol	Line Style
-	Solid
--	Dashed
:	Dotted
-.	Dash-dot

Symbol	Color
+	Plus sign
o	Circle
*	Asterisk
.	Point
x	Cross
s	Square
d	Diamond

Multiple data sets in one plot

- The command `hold on` holds the current plot and all axis properties so that subsequent graphing commands add to the existing graph.

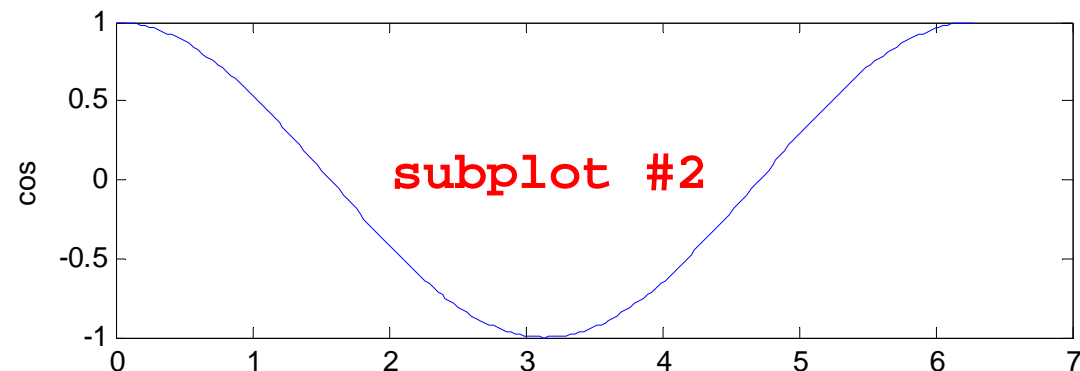
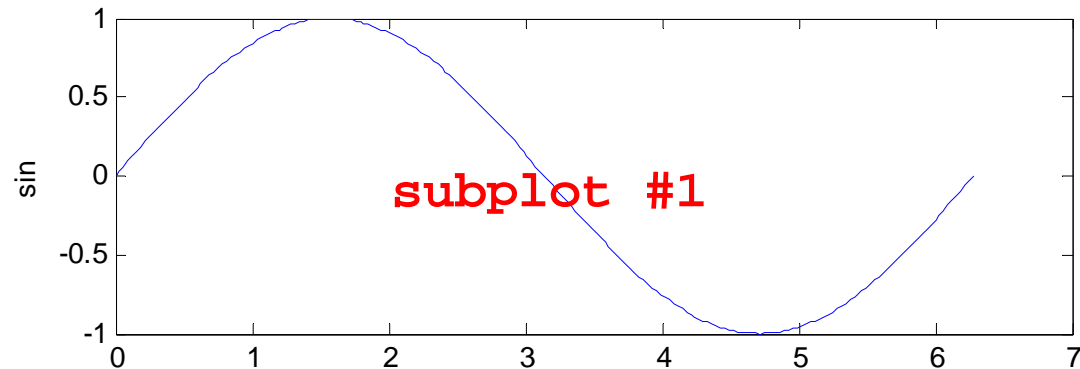


```
>> hold on  
>> plot(x, cos(x), 'r--')  
>> legend('sin', 'cos')
```

Multiple data sets in one plot

- The command `subplot(m,n,p)` breaks the Figure window into an m -by- n matrix of small axes, and selects the p -th axes for the current plot

```
>> subplot(2,1,1)
>> plot(x,sin(x))
>> ylabel('sin')
>> subplot(2,1,2)
>> plot(x,cos(x))
>> ylabel('cos')
```



Miscellaneous on plot

- The command **figure** opens a new figure or can be used to select a figure previously defined (**figure(FigNum)**)
- The command **close(FigNum)** closes a specific figure. The command **close all** closes all the figure defined in the MATLAB session
- The command **print** can be use to produce jpeg or eps images from the current figure

```
>> print -depsc FileName <----- It produces the file  
                               FileName.eps
```

```
>> print -djpeg FileName <----- It produces the file  
                               FileName.jpg
```

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